

Surface Area - Prisms and Cylinders

Tuesday, 13 March 2018 8:39 pm

By the end of the lesson I am asking for the following work to be completed:

Lesson	Lesson starter, examples, exercise	Proficiency/Enrichment	Standard	Advanced
6D	Surface area - prisms and cylinders Let's start: Drawing nets Key Ideas Example 10, 11	Understanding 1-2 Fluency 3-6 Problem-solving 7-10 Reasoning 11-14 Enrichment 15	2 3-4(4), 5 7-8(4) 11, 12	3-4(4), 5, 6 8(4), 9, 10 11-14

RECAP:

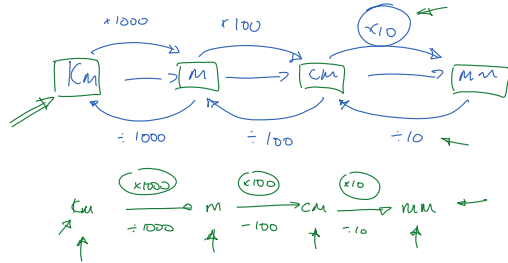
Measurement is a really important topic.

We have missed three important sections of this chapter which I will show a quick recap below.

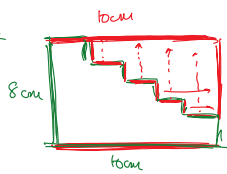
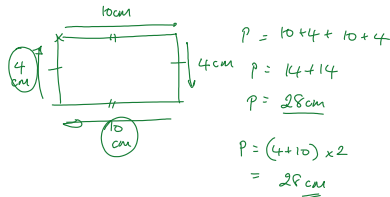
1. Review of Length
2. Pythagoras' Theorem
3. Area (Consolidating)

Review of Length

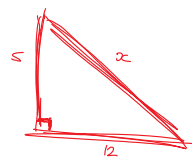
Converting between metric units of length i.e. km to m to cm to mm



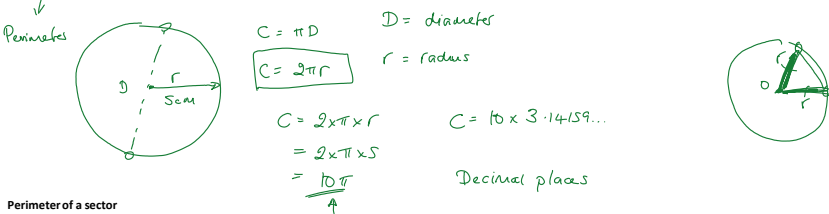
Perimeter



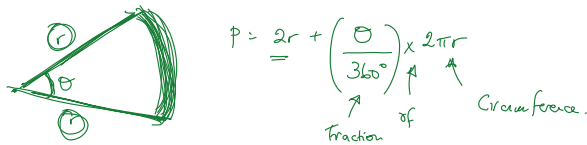
$P = 8 + 10 + 8 + 10$
 $= 18 + 18$
 $= 36cm$



Circumference of a Circle



Perimeter of a sector

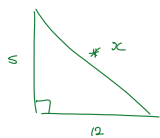


Review of Pythagoras' Theorem

I feel like we have done this to death!

However, we need to know that we can use Pythagoras' Theorem to find the Areas of Triangles!

As this whole chapter is about finding the areas of prisms and cylinders, here is a quick recap for Pythagoras' Theorem



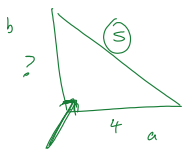
Perimeter?

$C^2 = a^2 + b^2$

$a^2 = b^2 + c^2$

$x^2 = 5^2 + 12^2$
 $x^2 = 25 + 144$
 $x^2 = 169$
 $x = \pm \sqrt{169}$
 $x = \pm 13$

$x = 13$ or ~~13~~

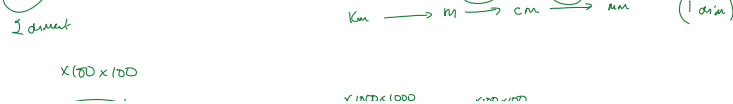


$C^2 = a^2 + b^2$
 $5^2 = 4^2 + ?^2$
 $25 = 16 + ?^2$

$?^2 = 25 - 16$ $? = \pm \sqrt{9}$
 $?^2 = 9$ $? = \pm 3$ $? = 3 \text{ units}$

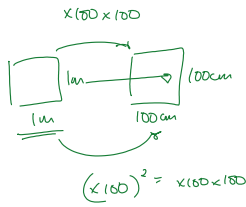
Area: Consolidating

Conversion of units of area i.e. km² to m² to cm² to mm²



1. convert

$$km \rightarrow m \rightarrow cm \rightarrow mm \quad (1 \text{ dir})$$

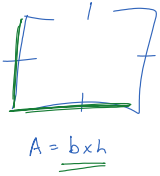


$$10000 \text{ cm}^2 \rightarrow 10000 \text{ m}^2 \rightarrow 10000 \text{ cm}^2 \rightarrow 10000 \text{ mm}^2$$

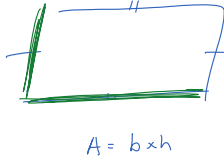
$$(10000)^2 \rightarrow (100)^2 \rightarrow (10)^2 \rightarrow 10000^2$$

Areas of standard shapes

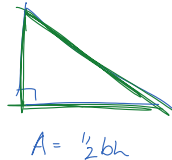
1. Square



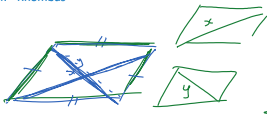
2. Rectangle



3. Triangle

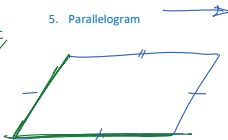


4. Rhombus



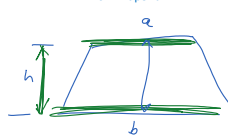
$$\text{Area} = \frac{1}{2}xy$$

5. Parallelogram



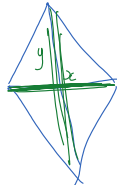
$$A = b \times h$$

6. Trapezium



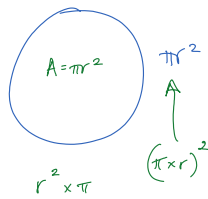
$$A = \frac{1}{2}(a+b)h$$

7. Kite

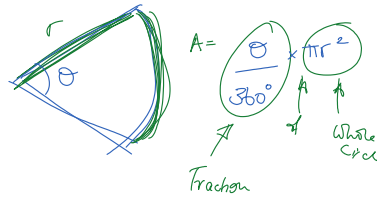


$$\text{Area} = \frac{1}{2}xy$$

8. Circle



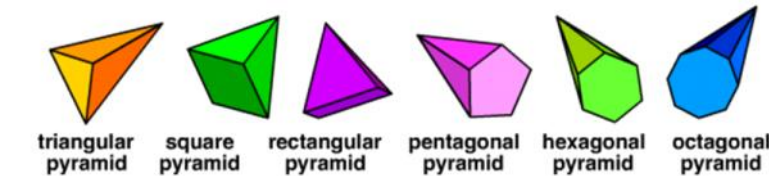
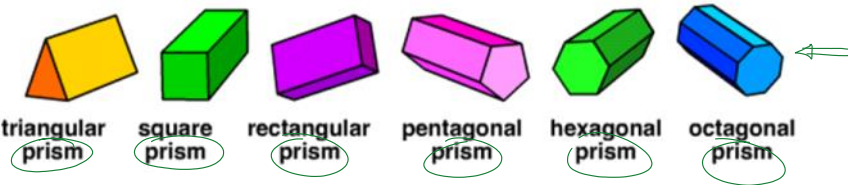
9. Area of a sector of a circle



Surface Area of Prisms and Cylinders ...

Firstly ... what is a prism?

It's a shape which, when oriented in a particular way, can be cut such that each slice would be identical in size. Examples include, cubes, cuboids, triangular prisms, cylinders etc. A pretty good selection is shown below.



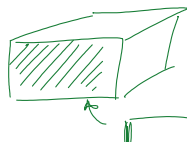
Secondly ... what is the surface area?

It's the sum of all the areas of all of the surfaces (faces) of a shape. This can apply to it being a prism or not!

To do this we need to view the shape as lots of surfaces (or faces). We find the area of each surface (or face) and then add them all together at the end.

There are lots of ways of doing this. Some more visual than others. Some more helpful than others. Which ever way you do it ... have a system!

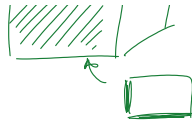
Back to the surface area



we find the area of each surface (or face) and then add them all together at the end.

There are lots of ways of doing this.
Some more visual than others.
Some more helpful than others.
Which ever way you do it ... have a system!

(E)
Back
Bottom
Side 1
Side 2



Lions and tigers and bears ... oh my!

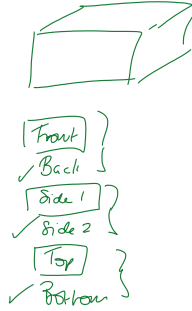
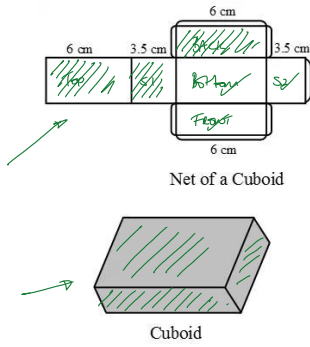
Not really ...
But we can think of the surface area of shapes as using the same building blocks of shapes:

Squares and triangles and circles ... oh my!



Finding Surface Areas of Cubes/Cuboids

This is considered the easiest of all shapes!
But it's the one which causes the most mistakes :(

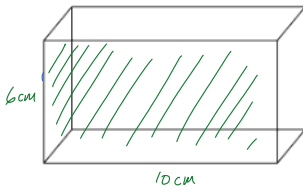


I like to save myself some time and work!



- A cuboid is effectively 6 faces:
- Top and bottom which are the same
 - Front and back which are the same
 - Left side and right side (which are the same!)

Total Surface Area



$$\begin{aligned}
 \text{Front} &= 6 \times 10 = 60 \text{ cm}^2 + \\
 \text{Back} &= 60 \text{ cm}^2 + \\
 \text{Top} &= + \\
 \text{Bottom} &= + \\
 \text{Side 1} &= + \\
 \text{Side 2} &= + \\
 \hline
 \text{T.S.A.} &= \underline{\hspace{2cm}}
 \end{aligned}$$

- This means I can find the area of:
1. The front
 2. The top
 3. One side
 4. Add them together
 5. Double it ...

Finding Surface Areas of Cylinders

This shape is awesome! Some of the greatest chocolates and lollies come in these shapes!!!

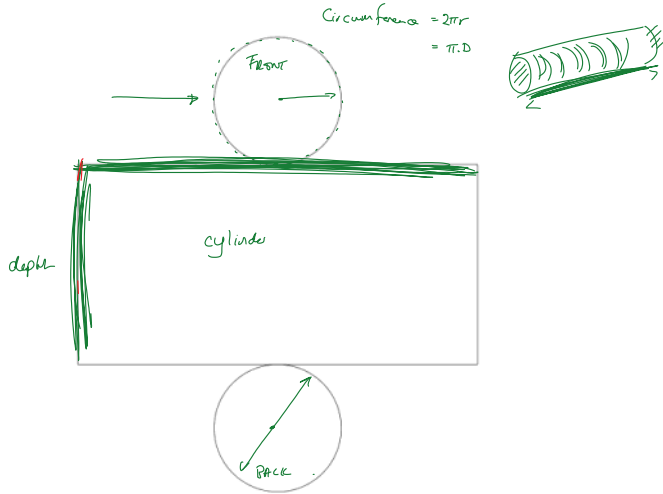


A cylinder is basically:

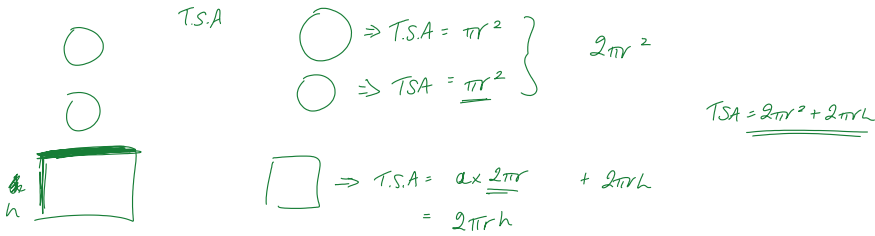
- Two circles (one at each end)
- A rectangle folded around it's shortest edge to meet itself.



In this case ... it's easier to see the net to see how we can find the surface area:



We use the idea that the circumference of a circle is πD to help us find the dimensions of one side of the rectangle. The other is given as the length of the cylinder.



Formula for the Surface Area of Cylinder (Closed) is $2\pi r^2 + 2\pi rh$
 This can also be factorised to become: $2\pi r(r+h)$

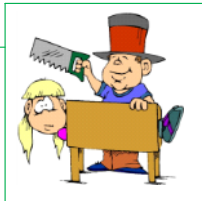
Maths is a BFT!

Remember, Maths is going to try and trick you!

All prisms can be described as:

- Open ended
- Closed ended

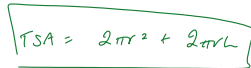
This makes a HUGE difference when working out the surface area.



Open = No ends!



Closed = ends

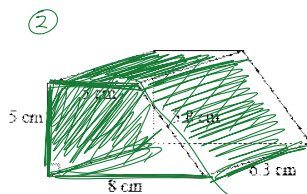
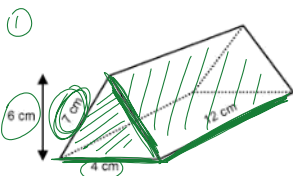


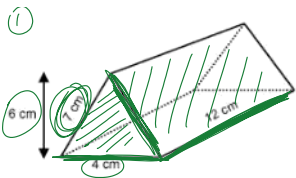
Finding Surface Areas of Prisms (General)

The basics are always the same.

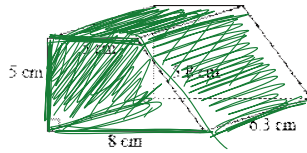
Split the shapes up into faces.

Find the areas of each of the faces and then add them together.

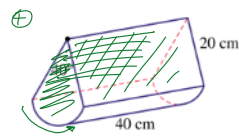
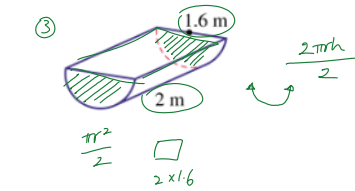
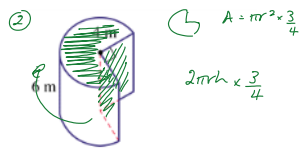
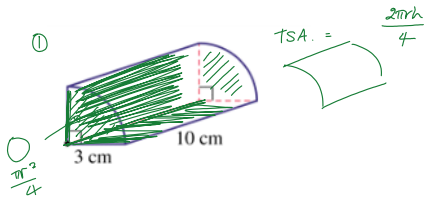




$$\begin{aligned} \text{Front} &= \frac{1}{2} \cdot b \cdot h = \frac{1}{2} \cdot 4 \cdot 6 = 12 \text{ cm}^2 \\ \text{Back} &= 12 \text{ cm}^2 \\ \text{Bottom} &= 12 \cdot 4 = 48 \text{ cm}^2 \\ \text{Face 1} &= 12 \cdot 7 = 84 \text{ cm}^2 \\ \text{Face 2} &= 12 \cdot 7 = 84 \text{ cm}^2 \\ \text{TSA} &= 12 + 12 + 48 + 84 + 84 \\ &= 24 + 48 + 168 \\ &= 72 + 168 \\ &= \underline{240 \text{ cm}^2} \end{aligned}$$



$$\begin{aligned} \text{Front} &= \frac{1}{2} \cdot (5+8) \cdot 5 \\ &= 32.5 \text{ cm}^2 \\ \text{Back} &= 32.5 \text{ cm}^2 \\ \text{Base} &= 8 \cdot 6.3 = \\ \text{Top} &= 5 \cdot 6.3 = \\ \text{Side} &= 5 \cdot 6.3 = \\ \text{Side} &= 5 \cdot 8 \cdot 6.3 = \end{aligned}$$



$$\text{Area} = \frac{40^\circ}{360^\circ} \times \pi r^2 \times 2$$

Fraction

$$\rightarrow 2\pi r h \times \frac{40^\circ}{360^\circ}$$

What about when we have shapes sitting on shapes.
Easy! Find the surface area of each shape separately, then take away the areas where they overlap!

