माध्यमिक शिक्षा परीक्षा

(Secondary Education Examinations - SEE) अनिवार्य गणित

समय : 3:00 घण्टा पूर्णाङ्ग : 100

सबै प्रश्नहरूहलगर्नुहोस् । Attempt all the Questions.

समूह 'क' (Group 'A') [3 x 2 = 6]

1. a) यदि कुनै सामानको शुरुको मूल्य रे. Pर वार्षिक ह्रासदर R% छ भने T वर्ष पछिको मूल्य पत्ता लगाउने सुत्र लेख्नुहोस् ।

If the initial price of an article is Rs. P and annual rate of depreciation is R%, then write the formula to find the price after T years.

b) एउटा समद्धिबाहु त्रिभुजको आधार भुजा b से.मी. र बराबर दुई भुजाहरु a से.मी. छन् भने उक्त त्रिभुजको क्षेत्रफल कित हुन्छ ? लेख्नुहोस् ।

The base of an isosceles triangle is b cm and equal sides are a cm. What is the area of the triangle? Write it.

2. a) ल.स. को परिभाषा लेख्नुहोस् । Define L.C.M.

b) यदि कुनै तथ्याङ्कको मध्यका श्रेणीको तल्लो सीमा L, सो श्रेणीको बारम्बारता f, श्रेणी अन्तर i, वारम्वारताहरुको जोड N र मध्यका श्रेणीभन्दा अघिल्लो श्रेणीको सञ्चित बारम्बारता cf छन् भने मध्यिका (Md) पत्ता लगाउने सूत्र लेख्नुहोस् ।

If the lower limit of the median class of any data is L, frequency of that class is f, class interval i, sum of the frequencies N and the cumulative frequency of pre-median class is cf, then write the formula for finding the median (Md).

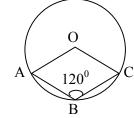
 a) एउटै आधार र उही समानान्तर रेखाहरू बीच रहेका आयत र त्रिभुजका क्षेत्रफलहरु बीचको सम्बन्ध लेख्नुहोस्।

Write the relationship between the areas of a rectangle and a triangle standing on the same base and between the same parallel lines.

b) दिइएको चित्रमा O वृत्तको केन्द्र हो । यदि $\angle ABC = 120^0$

भए वृहत ∠AOC को नाप कित हुन्छ ? लेख्नुहोस्। In the given figure O is the centre of the circle. If

 $\angle ABC = 120^{\circ}$, what is the size of the reflex $\angle AOC$? Write it.



समूह 'ख' (Group 'B') [7 x (2+2) +3 x (2+2+2) =34]

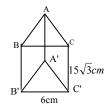
4. a) नेपाल राष्ट्र बैंकको मुद्रा विनिमय दर अनुसार अमेरिकन डलर 1 को खरीद दर र बिक्रीदर क्रमश: नेपाली रु. 103.72 र रु. 104.32 छन भने :

According to the money exchange rate of Nepal Rastra Bank, the purchasing and selling rates of 1 American dollar are NRs.103.72 and NRs. 104.32 respectively, Then.

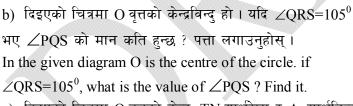
- i) नेपाली रु. 57,376 संग कित अमेरिकन डलर साट्न सिकन्छ ? How many American dollars can be exchanged with NRs. 57,376 ?
- ii) तपाईंले \$500 संग कित नेपाली रुपैयाँ साट्न सक्नुहुन्छ ? पत्ता लगाउनुहोस् । How much Nepali rupees can you exchange with \$500 ? Find it.
- b) वि.सं.2072 को शुरुमा एउटा शहरको जनसंख्या 50,000 थियो । यदि वार्षिक जनसङ्ख्या वृद्धिदर 10% छ

भने वि.सं. 2074 को अन्तमा त्यो शहरको जनसङ्ख्या कित होला ? पत्ता लगाउनुहोस्। In the beginning of 2072 B.S., the population of a town was 50,000. If the annual population growth rate is 10%, what will be the population of the town at the end of 2074 B.S. ? Find it.

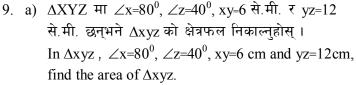
- 5. a) भुजाहरु 3से.मी., 4से.मी. र 5 से.मी. भएको एउटा त्रिभुजको क्षेत्रफल निकाल्नुहोस्। Find the area of a triangle with sides 3 cm, 4 cm and 5 cm.
 - b) दिइएको समबाहु त्रिभुजाकार प्रिज्ममा B'C'= 6 से.मी.र $CC' = 15\sqrt{3}$ से.मी. छन् भने सो प्रिज्मको आयतन पत्ता लगाउनुहोस्। In the given equilateral triangular prism B'C'=6cm and $CC' = 15\sqrt{3}$ cm. Find the volume of the prism.



- c) यदि एउटा गोलाको आयतन 4851 घन से.मी. छ भने यसको व्यास निकाल्नुहोस्। If the volume of a sphere is 4851 cubic cm find its diameter.
- 6. a) x^4 -x र x^2 +x+1 को म.स. पत्ता लगाउनुहोस्। Find the H.C.F. of x^4 - x and x^2 + x+ 1
 - b) सरल गर्नुहोस् : (Simplify) : $\sqrt[3]{16} + \sqrt[3]{54} \sqrt[3]{250}$
- 7. a) के समीकरण $\sqrt{2x-1}=-1$ को एकल समाधान हुन्छ, कि हुँदैन ? जाँच गर्नुहोस् । Whether the equation $\sqrt{2x-1}=-1$ has a unique solution or not ? Check it.
 - b) सरल गर्नुहोस् : (Simplify) : $\frac{1}{1-x^{b-a}} + \frac{1}{1-x^{a-b}}$
 - c) यदि तीनवटा क्रमागतः जोर संख्याहरुको योगफल 36 छ भने ती संख्याहरु पत्ता लगाउनुहोस्।
 If the sum of three consecutive even numbers is 36, find the numbers.
- 8. a) दिइएको चित्रमा BC को मध्यविन्दु D हो र DE⊥AC छ । यदि AC=12 से.मी. र DE=5 से.मी. छन् भने ∆ABC को क्षेत्रफल निकाल्नुहोस् ।
 In the given figure D is the mid-point of BC and DE⊥AC. If AC=12cm and DE=5cm. find the area of ∆ABC.

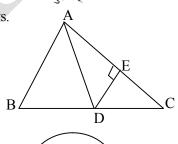


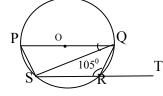
c) दिइएको चित्रमा O वृत्तको केन्द्र, TN स्पर्शरेखा र A स्पर्शविन्दु हुन्। यदि $\angle AOB=80^{0}$ भए $\angle BAT$ को नाप पत्तालगाउनुहोस्। In the given figure O is the centre of the circle, TN, the tangent and A is the point of contact. If $\angle AOB=80^{0}$, find the measurement of $\angle BAT$.

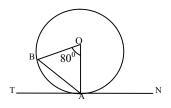


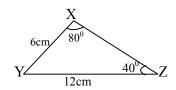
b) एउटा निरन्तर श्रेणीमा यदि मध्यक (x) = 6, $\sum fm=72+8k$ र $\sum f=16+k$ भए जम्मा पदहरुको संख्या पत्ता लगाउनुहोस् ।

In a continuous series, if the mean $(\bar{x}) = 6$, $\sum \text{fm} = 72 + 8k$ and $\sum \text{f} = 16 + k$, find the total number









of terms.

 एउटा डाइस र एउटा सिक्का एकैसाथ उफार्दा डाइसमा रुढ संख्या र सिक्कामा शीर आउने सम्भाव्यता पत्ता लगाउनुहोस् ।

Find the probability of getting a prime number on the dice and head on the coin when a dice is rolled and a coin is tossed simultaneously.

b) राम्ररी फिटिएको 52 पत्तीको एक प्याकेट तासबाट नहेरीकन एकपछि अर्को पुनः नराखीकन दुइवटा तास भिक्तिएका छन्। वृक्षचित्र खिची अनुहार भएको तास पर्ने र नपर्ने सबै सम्भावित परिणामहरूको सम्भाव्यताहरूलाई देखाउनुहोस्।

Two cards are drawn randomly in succession without replacement from a well shuffled pack of 52 cards. By drawing a tree diagram show the probabilities of all the possible outcomes of getting and not getting a faced card.

समूह 'ग' (Group' C') [10x4=40]

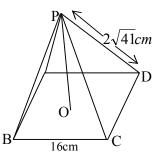
11. 50 जना विद्यार्थीहरूको एक समूहमा 20 जनाले गणित मात्र र 15 जनाले विज्ञान मात्र मन पराउँछन्। यदि यी दुई विषयहरू मध्ये कुनै पिन विषय मन नपराउने विद्यार्थीहरूको संख्या दुवै विषय मन पराउने विद्यार्थीहरूको संख्याभन्दा दोब्बर छन् भने भेन चित्र प्रयोग गरेर बढीमा एउटा विषय मन पराउने विद्यार्थीहरूको संख्या पत्तालगाउन्होस्।

In a group of 50 students 20 like only Maths and 15 like only Science. If the number of students who do not like any of the two subjects is double of the number of students who like both subjects, find the number of students who like at most one subject by using a Venn-diagram.

12. एकजना पर्यटकले 20% छुट र 13% मूल्य अभिवृद्धिकरसिंहत एउटा नेपाली टोपी किनेछन् । आफ्नो देश फर्कंदा उनलाई विमानस्थलमा मूल्यअभिवृद्धिकर रकम रु.83.20 फिर्ता दिईयो भने सो टोपीको अङ्कितमूल्य कित रहेछ ? पत्ता लगाउन्होस् ।

A tourist bought a Nepali cap with 20% discount and 13% value added tax. When returning to his country the VAT amount Rs. 83.20 returned back to him at the airport. What was the marked price of the cap? Find it.

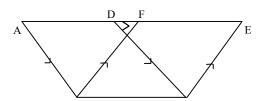
13. दिइएको चित्र एउटा वर्गाकार आधार भएको ठोस पिरामिडको हो । यदि आधार भुजाको लम्बाई (BC) 16 से.मी. र छड्के किनाराको लम्बाई (PD) $2\sqrt{41}$ से.मी.भए सो पिरामिडको आयतन पत्ता लगाउनुहोस् । The given figure is of a solid square based pyramid. If the length of side of the base (BC) is 16cm and the length of the lateral edge (PD) is $2\sqrt{41}$ cm, find the volume of the pyramid.



14. सरल गर्नुहोस् : (Simplify) :
$$\frac{x+2}{x^2+2x+4} + \frac{x-2}{x^2-2x+4} + \frac{16}{x^4+4x^2+16}$$

15. रु.1000 केही मानिसहरुलाई बराबरी हुनेगरी बाँडियो। यदि 5 जना मानिसहरु बढी भएको भए प्रत्येकले रु.10 कम पाउने थिए भने कतिजना मानिसहरुलाई सो रकम बाँडिएको थियो? पत्तालगाउनुहोस्। Rs. 1000 was distributed equally among a certain number of people. If there were 5 people more, each would have received Rs. 10 less. Among how many people was the amount distributed? Find it.

16. दिइएको चित्रमा AE||BC, AB||DC र BF||CE छन् भने, प्रमाणित गर्नुहोस् :
In the given figure, AE||BC, AB||DC and BF||CE, then prove that :



i) $\triangle ABF \cong \triangle DCE$

C

- ii) □ ABCD = □ FBCE
- 17. आधार BC=6 से.मी. र उचाइ AD=4 से.मी. भएको एउटा समद्धिबाह त्रिभुज ABC रचना गर्नुहोस् । त्रिभुज ABC को क्षेत्रफलसँग बराबर हुनेगरी एउटा कोण CDE=450 भएको एउटा समानान्तर चत्र्भ्ज CDEF को रचना पनि गर्नुहोस् ।

Construct an isosceles triangle ABC having base BC=6cm and the altitude AD=4cm. Also construct a parallelogram CDEF equal in area to \triangle ABC and having one angle CDE=45°.

18. एउटै वृत्तखण्डका कोणहरु बराबर हुन्छन् भनी प्रयोगद्वारा परीक्षण गर्नुहोस् । (कम्तीमा 3 से.मी. अर्धव्यास भएका द्ईवटा वृत्तहरु आवश्यक छन्।)

Verify experimentally that the angles in the same segment of a circle are equal. (Two circles having radii at least 3cm are necessary.)

19. एउटा घरको छतबाट 20 फीट अग्लो एउटा रुखको ट्प्पोको अवनित कोण 30^0 पाइयो । यदि घर र रुखबीचको दूरी $10\sqrt{3}$ फीट छ भने घरको उचाई पत्ता लगाउन्होस् ।

From the roof of a house the angle of depression of the top of a tree 20ft. high was found to be 30°. If the distance between the house and the tree is $10\sqrt{3}$ ft, find the height of the house.

20. दिइएको तथ्याङ्कको पहिलो चत्थांश 35 भए x को मान पत्तालगाउन्होस् ।

The first quartile of the given data is 35, find the value of x.

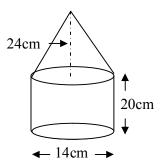
1	-					
प्राप्ताङ्ग (Marks Obtained)		0-20	20-40	40-60	60-80	80-100
विद्यार्थी संख्या (No of Students)		2	X	8	5	1

समूह 'घ' (Group D) [4x5 =20] 21. कुनै धन 3 वर्षसम्म वार्षिक 10% ले साधारण ब्याजमा राखियो र त्यसपछिको मिश्रधनलाई सोही दरमा 2 वर्षसम्म चक्रीय व्याजमा लगानी गरियो। यदि 5 वर्षमा जम्मा मिश्रधन रु. 471,900 भयो भने मुलधन कति थियो ? पत्ता लगाउनहोस् ।

A sum of money is placed at simple interest for 3 years at 10% per annum and then the amount is invested for 2 years at the same rate at compound interest. If the total amount of 5 years became Rs. 471,900, what was the sum? Find it.

22. दिइएको चित्र एउटा सोली र बेलना मिली बनेको ठोस वस्तुको हो। यदि बेलना र सोलीको उचाईहरु ऋमशः 20 से.मी. र 24 से.मी. छन् र आधारको व्यास 14 से.मी. छ भने उक्त वस्त्को पूरा सतहको क्षेत्रफल निकाल्न्होस् ।

The given figure is of a solid object made up of a cone and a cylinder. If the heights of the cylinder and cone are 20cm and 24cm respectively and the diameter of the base is 14cm, find the total surface area of the object.



23. यदि $x^2 - 2 = 2^{\frac{2}{3}} + 2^{\frac{-2}{3}}$ भए, प्रमाणित गर्नुहोस् :

If $x^2 - 2 = 2^{\frac{2}{3}} + 2^{\frac{-2}{3}}$, then prove that:

i)
$$x = 2^{\frac{1}{3}} + 2^{\frac{-1}{3}}$$

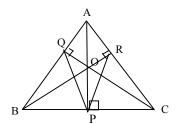
ii)
$$2x^3-6x=3$$

24. दिइएको चित्रमा AP⊥BC, BR⊥AC र CQ⊥AB छन् भने,

प्रमाणित गर्नहोस : ∠OPO=∠OPR

In the given figure, AP \perp BC, BR \perp AC and CQ \perp AB.

Prove that : $\angle OPQ = \angle OPR$



Marking Schemes

1. (a) (i)
$$P_T = P\left(1 - \frac{R}{100}\right)^T$$
 (1)
(b) (i) Area of isosceles triangle $= \frac{b}{4}\sqrt{4a^2 - b^2}$ (1)
2. (a) (i) Lowest Common Multiple (1)
(b) $Md = L + \left(\frac{N}{2} - cf\right) \times \frac{i}{f}$ (1)
3. (a) (i) Ar. of rectangle= $2 \times Ar$. of triangle. (1)
(b) (i) Reflex $\angle AOC = 240^0$ (1)
4. (a) (i) \$550 (1)
(ii) Rs. 51,860 (1)
(b) (i) $P_T = 50,000 \left(1 + \frac{10}{100}\right)^3$ (1)
(ii) $P_T = 66550$ (1)
(iii) $A = \frac{1}{2} \times 3 \times 4 = 6cm^2$ (1)
(b) (i) Base $A = \frac{\sqrt{3}}{4} \times 6^2 = 9\sqrt{3}cm^2$ (1)
(ii) $Vol. = 9\sqrt{3} \times 15\sqrt{3} = 405 cm^3$ (1)
(ii) Diameter = 21 cm (1)
(ii) Diameter = 21 cm (1)
(ii) \therefore H.C.F. = $x^2 + x + 1$ (1)
(ii) \therefore H.C.F. = $x^2 + x + 1$ (1)
(ii) Checking \therefore 1 \neq -1 (1)
(ii) Checking \therefore 1 \neq -1 (1)
(ii) 1 (1) (1)
(iii) 2x + (2x + 2) + (2x + 4) = 36 (1)

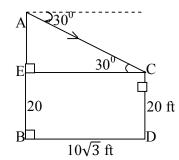
(ii) 1 ---- (1)
(c) (i)
$$2x + (2x + 2) + (2x + 4) = 36$$
 ---- (1)
(ii) Regd. Nos are 10, 12, 14 ---- (1)
8. (a) (i) $\triangle ADC = 30 \text{ cm}^2$ ---- (1)
(ii) $\triangle ABC = 60 \text{ cm}^2$ ---- (1)
(b) (i) $\angle P = 75^0$ ---- (1)
(ii) $\angle PQS = 15^0$ ---- (1)
(c) (i) $\angle OAB = 50^0$ ---- (1)
(ii) $\angle BAT = 40^0$ ---- (1)
9. (a) (i) $\angle y = 60^0$ ---- (1)
(ii) $\triangle xyz = \frac{1}{2}6 \times 12 \times \frac{\sqrt{3}}{2} = 18\sqrt{3}cm^2$ ---- (1)
(b) (i) $K = 12$ ---- (1)

- 10. (a) (i) $P(Prime) = \frac{3}{6} = \frac{1}{2}$ $P(H) = \frac{1}{2}$ (ii) $P(Prime \cap H) = \frac{1}{4}$ ---- (1)
- (b) N = Non Face Card. F F = Face Card. F 12/52 40/51 F 12/51 F
- 11. (i) Fig + description ---- (1+1)
 - (ii) 20 + x + 15 + 2x = 50 $\therefore x = 5$ ---- (1)
 - (iii) $n(\overline{M \cap S}) = 45$ ---- (1)
- 12. (i) 13% of SP = 83.20 ---- (1)
 - (ii) Sp=640 ---- (1)
 - (iii) 80% of M.P.= 640 (1) (iv) \therefore M.P. = Rs. 800 (1)
- 13. (i) Slant ht. $l = \sqrt{(2\sqrt{41})^2 8^2}$ = 10 cm. (1)
 - (ii) Vertical ht. $(h) = \sqrt{10^2 8^2}$ = 6 cm ---- (1)
- 13. (iii) $V = \frac{1}{3} \times 16^2 \times 6$ ---- (1)
 - (iv) :: v = 512 c.c. (1)
- 14. (i) $\frac{x^3 + 2^3 + x^3 2^3}{(x^2 + 2x + 4)(x^2 2x + 4)} + \frac{16}{x^4 + 4x^2 + 16}$ ---- (1)
 - (ii) $\frac{2x^3}{x^4 + 4x^2 + 16} + \frac{16}{x^4 + 4x^2 + 16}$ ---- (1)
 - (iii) $\frac{2(x+2)(x^2-2x+4)}{(x^2+2x+4)(x^2-2x+4)}$ ---- (1)
 - (iv) $\frac{2(x+2)}{(x^2+2x+4)}$ ---- (1)
- 15. (i) Let no. of people be x. then, each received Rs. $\frac{1000}{x}$ ---- (1)
 - (ii) No. of men = x + 5 ---- (1) $\therefore \text{ each received Rs. } \frac{1000}{x + 5}$
 - (iii) $\frac{1000}{x} \frac{1000}{x+5} = 10$ ---- (1)
 - (iv) $\therefore x = 20$ ---- (1)
- 16. (i) $\triangle ABF \cong \triangle DCE$ ---- (1+1)
 - (ii) $\triangle ABF = \triangle DCE$ ---- (1)
 - (iii) $\square ABCD = \square FBCE$ ---- (1)

(1)

(1)

- 17. (i) For construction of $\triangle ABC$ ---- (1)
 - (ii) Drawing a line parallel to BC. ---- (1)
 - (iii) Drawing angle 45° . ---- (1)
 - (iv) For construction \(\subseteq \text{CDEF} \) ---- (1)
- 18. (i) For correct figures. ---- (1)
 - (ii) For correct measurements. ---- (1+1)
 - (iii) Conclusion. ---- (1)
- 19. (i) For correct figure and description ---- (1)



(ii) Tan
$$30^0 = \frac{AE}{EC}$$

$$\therefore \frac{1}{\sqrt{3}} = \frac{AE}{10\sqrt{3}}$$

(iii) ::
$$AE = 10 \text{ ft.}$$
 (1)

(ii)
$$Q_1 \text{ class} = 20-40$$

(iii)
$$35 = 20 + \left(\frac{16+M}{4} - 2\right) \times \frac{20}{x}$$
 ---- (1)

(iv)
$$:: x = 4$$
 ---- (1)

21. (i) Let
$$p = Rs. x$$

$$\therefore SI = \frac{x \times 3 \times 10}{100} = \frac{3x}{10}$$
---- (1)

(ii) Amount =
$$x + \frac{3x}{10} = \frac{13x}{10}$$
 ---- (1)

(iii)
$$471900 = \frac{13x}{10} \left(1 + \frac{10}{100}\right)^2$$
 ---- (1)

(iv)
$$\therefore x = Rs.300,000$$
 ---- (1)

22. (i) For finding height of cone. ---- (1) ie,
$$h = \sqrt{25^2 - 7^2} = 24 \text{ cm}$$

(ii) CSA of cone
$$=\frac{22}{7} \times 7 \times 25$$

=550cm² ---- (1)

$$-350 \text{cm}$$
(iii) CSA of cylinder= $2 \times \frac{22}{7} \times 7 \times 20$

$$=880 \text{ cm}^2 \qquad ---- \qquad (1)$$

(iv) Base Area =
$$\frac{22}{7} \times 7^2$$

= 154 cm² ---- (1)

(v) Total surface area =
$$1584 \text{ cm}^2$$
 ---- (1)

23. (i) For
$$x^2 = (2^{1/3})^2 + 2 \cdot 2^{1/3} \cdot 2^{-1/3} + (2^{-1/3})^2$$
 ---- (1)

(ii)
$$\therefore x = 2^{1/3} + 2^{-1/3}$$
 ---- (1)

	(iii)	$x^3 = 2 + \frac{1}{2} + 3(2^{1/3} + 2^{-1/3})$	 (1)
	(iv)	$x^3 = \frac{4+1+6x}{2}$	 (1)
	(v)	$\therefore 2x^3 - 6x = 5$	 (1)
24.	(i)	PORC and POQB are cyclic quads.	 (1)
	(ii)	B, C, R and Q are concyclic pts.	 (1)
	(iii)	$\angle OPR = \angle OCR$ and	
		∠OPQ = ∠OBQ	 (1)
	(iv)	$\angle OBQ = \angle OCR$	 (1)
	(v)	$\therefore \angle OPQ = \angle OPR$	 (1)

MMM